

All of the addition properties of real numbers that you learned in Lesson 1-4 apply to both positive and negative numbers. You can use these properties to reorder and simplify expressions.

Problem 4 Adding and Subtracting Real Numbers

Scuba Diving A reef explorer dives 25 ft to photograph brain coral and then rises 16 ft to travel over a ridge before diving 47 ft to survey the base of the reef. Then the diver rises 29 ft to see an underwater cavern. What is the location of the cavern in relation to sea level?

Think

How do you represent the problem with an expression?
Start your expression with zero to represent sea level. Subtract for dives, and add for rises.

Know

Distance and direction for each change in location

Need

Location in relation to sea level after changes

Plan

Represent the diver's trip with an expression. Reorder the values to make calculations easier.

$$0 - 25 + 16 - 47 + 29$$

$$= 0 + (-25) + 16 + (-47) + 29$$

$$= 0 + 16 + 29 + (-25) + (-47)$$

$$= 0 + (16 + 29) + [(-25) + (-47)]$$

$$= 0 + 45 + (-72)$$

$$= 45 + (-72)$$

$$= -27$$

Write an expression.

Use rule for subtracting real numbers.

Commutative Property of Addition


Group addends with the same sign.

Add inside grouping symbols.

Identity Property of Addition

Use rule for adding numbers with different signs.

The cavern is at -27 ft in relation to sea level.

 **Got It?** 4. A robot submarine dives 803 ft to the ocean floor. It rises 215 ft as the water gets shallower. Then the submarine dives 2619 ft into a deep crevice. Next, it rises 734 ft to photograph a crack in the wall of the crevice. What is the location of the crack in relation to sea level?



Lesson Check

Do you know HOW?

Use a number line to find each sum.

1. $-5 + 2$

2. $-2 + (-1)$

Find each sum or difference.


3. $-12 + 9$

4. $-4 + (-3)$


5. $-3 - (-5)$

6. $1.5 - 8.5$

Do you UNDERSTAND? MATHEMATICAL PRACTICES

 7. **Vocabulary** What is the sum of a number and its opposite?

 8. **Compare and Contrast** How is subtraction related to addition?

 9. **Error Analysis** Your friend says that since $-a$ is the opposite of a , the opposite of a number is always negative. Describe and correct the error.



Practice and Problem-Solving Exercises



MATHEMATICAL PRACTICES

A Practice

Use a number line to find each sum.

10. $2 + 5$

11. $-3 + 8$

12. $4 + (-3)$

13. $1 + (-6)$

14. $-6 + 9$

15. $-4 + 7$

16. $-6 + (-8)$

17. $-9 + (-3)$

Find each sum.

18. $11 + 9$

19. $17 + (-28)$

20. $12 + (-9)$

21. $-2 + 7$

22. $-14 + (-10)$

23. $-9 + (-2)$

24. $3.2 + 1.4$

25. $5.1 + (-0.7)$

26. $-2.2 + (-3.8)$

27. $\frac{1}{2} + \left(-\frac{7}{2}\right)$

28. $-\frac{2}{3} + \left(-\frac{3}{5}\right)$

29. $\frac{7}{9} + \left(-\frac{5}{12}\right)$

Find each difference.

30. $5 - 15$

31. $-13 - 7$

32. $-19 - 7$

33. $36 - (-12)$

34. $-29 - (-11)$

35. $-7 - (-5)$

36. $8.5 - 7.6$

37. $-2.5 - 17.8$

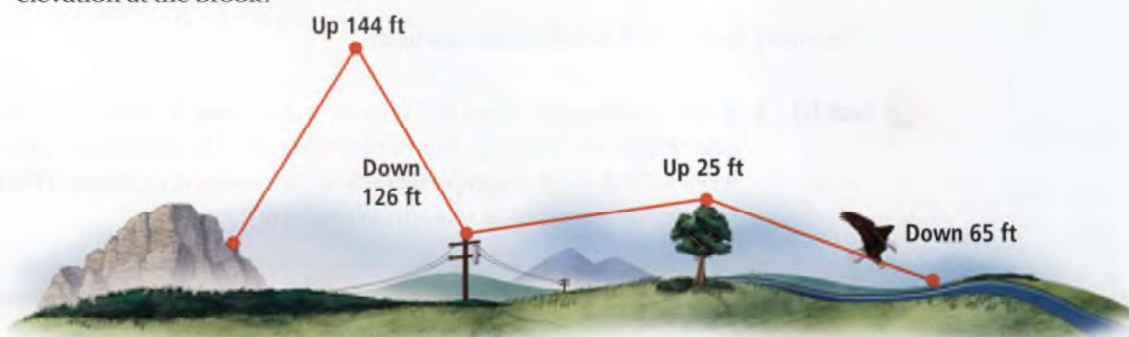
38. $-2.9 - (-7.5)$

39. $3.5 - 1.9$

40. $\frac{1}{8} - \frac{3}{4}$

41. $\frac{7}{16} - \left(-\frac{1}{2}\right)$

42. **Bird Watching** An eagle starts flying at an elevation of 42 ft. Elevation is the distance above sea level. The diagram below shows the elevation changes during the eagle's flight. Write an expression representing the eagle's flight. What is the elevation at the brook?



43. **Stock Market** A stock's starting price per share is \$51.47 at the beginning of the week. During the week, the price changes by gaining \$1.22, then losing \$3.47, then losing \$2.11, then losing \$.98, and finally gaining \$2.41. What is the ending stock price?

B Apply

Evaluate each expression for $a = -2$, $b = -4.1$, and $c = 5$.

44. $a - b + c$

45. $-c + b - a$

46. $-a + (-c)$

47. **Error Analysis** Describe and correct the error in finding the difference shown at the right.
48. **Writing** Without calculating, tell which is greater, the sum of -135 and 257 or the sum of 135 and -257 . Explain your reasoning.

$$\begin{aligned} -4 - (-5) &= -4 + (-(-5)) \\ &= -4 + 5 \\ &= -1 \end{aligned}$$

Simplify each expression.

49. $1 - \frac{1}{2} - \frac{1}{3} - \frac{1}{4}$

50. $7 + (2^2 - 3^2)$

51. $-2.1 - [2.3 - (3.5 - (-1.9))]$

- © 52. **Think About a Plan** In golf, the expected number of strokes is called “par.” When the number of strokes taken is more than par, your score is positive. When the number of strokes is less than par, your score is negative. The lowest score wins.

The scorecard shows par and one golfer’s score for the first four holes played on a nine-hole golf course. The golfer’s scores on the remaining five holes are $-1, 0, -1, +1, 0$. Par for the nine holes is 36. What is the golfer’s total number of strokes for the nine holes?

- Can you solve the problem by adding the strokes taken on each hole?
- How is the sum of the golfer’s scores related to the total number of strokes taken?

Golf Scorecard

Par	Number of Strokes	Score
4	6	+2
4	3	-1
3	3	0
5	3	-2

- © Reasoning Use reasoning to determine whether the value of each expression is positive or negative. Do not calculate the exact answers.

53. $-225 + 318$

54. $-\frac{7}{8} + \frac{1}{3}$

55. $34.5 + 12.9 - 50$

- STEM 56. **Temperature Scales** The Kelvin temperature scale is related to the degrees Celsius ($^{\circ}\text{C}$) temperature scale by the formula $x = 273 + y$, where x is the number of kelvins and y is the temperature in degrees Celsius. What is each temperature in kelvins?

a. -22°C

b. 0°C

c. -32°C

- © 57. **Writing** Explain how you can tell without calculating whether the sum of a positive number and a negative number will be positive, negative, or zero.

Decide whether each statement is true or false. Explain your reasoning.

58. The sum of a positive number and a negative number is always negative.
59. The difference of two numbers is always less than the sum of those two numbers.
60. A number minus its opposite is twice the number.

- STEM 61. **Meteorology** Weather forecasters use a barometer to measure air pressure and make weather predictions. Suppose a standard mercury barometer reads 29.8 in. The mercury rises 0.02 in. and then falls 0.09 in. The mercury falls again 0.18 in. before rising 0.07 in. What is the final reading on the barometer?

62. **Multiple Choice** Which expression is equivalent to $x - y$?

(A) $y - x$

(B) $x - (-y)$

(C) $x + (-y)$

(D) $y + (-x)$

- STEM 63. **Chemistry** Atoms contain particles called protons and electrons. Each proton has a charge of $+1$ and each electron has a charge of -1 . A certain sulfur ion has 18 electrons and 16 protons. The charge on an ion is the sum of the charges of its protons and electrons. What is the sulfur ion’s charge?