

Name:	Date:
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Topic:	Class:
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Main Ideas/Questions	Notes/Examples	
<b>STATEMENT</b>	<ul style="list-style-type: none"> <li>A statement is a sentence that is either _____ or _____.</li> <li>This is called the _____.</li> <li>Represented using letters such as _____ or _____</li> </ul>	
	<table border="1"> <tr> <td><b>EXAMPLE:</b> <math>p</math>: Supplementary angles have a sum of <math>180^\circ</math>.</td> <td><b>Truth Value:</b></td> </tr> </table>	<b>EXAMPLE:</b> $p$ : Supplementary angles have a sum of $180^\circ$ .
<b>EXAMPLE:</b> $p$ : Supplementary angles have a sum of $180^\circ$ .	<b>Truth Value:</b>	
<b>NEGATION</b>	<ul style="list-style-type: none"> <li>A negation of a statement has the _____ truth value.</li> <li>Shown by the symbol _____. ← <span style="border: 1px solid black; border-radius: 10px; padding: 2px;">Read as "not <math>p</math>"</span></li> </ul>	
	<table border="1"> <tr> <td><b>EXAMPLE:</b> <math>\sim p</math>: Supplementary angles do not have a sum of <math>180^\circ</math>.</td> <td><b>Truth Value:</b></td> </tr> </table>	<b>EXAMPLE:</b> $\sim p$ : Supplementary angles do not have a sum of $180^\circ$ .
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<b>COMPOUND</b> <i>Statements</i>		
<b>CONJUNCTION</b>	<ul style="list-style-type: none"> <li>Statements joined by the word _____.</li> <li>Written as <math>p</math> ____ <math>q</math>.</li> <li>True when _____ statements are _____.</li> </ul>	
<b>DISJUNCTION</b>	<ul style="list-style-type: none"> <li>Statements joined by the word _____.</li> <li>Written as <math>p</math> ____ <math>q</math>.</li> <li>True when _____ statement is _____.</li> </ul>	

**Directions:** Write compound statements using the statements below and determine each truth value.

$p$ : There are seven days in a week.       $q$ : March has exactly 30 days.       $r$ : Halloween is on October 31<sup>st</sup>.

1.  $p \wedge q$ : \_\_\_\_\_  
 \_\_\_\_\_ Truth Value: \_\_\_\_\_

2.  $q \wedge r$ : \_\_\_\_\_  
 \_\_\_\_\_ Truth Value: \_\_\_\_\_

3.  $p \wedge r$ : \_\_\_\_\_  
 \_\_\_\_\_ Truth Value: \_\_\_\_\_

4.  $\sim p \wedge q$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

5.  $p \vee r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

6.  $\sim q \vee r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

7.  $\sim p \vee \sim r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

8.  $\sim p \vee \sim q$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

**Write your own!**

$p$ : \_\_\_\_\_

$q$ : \_\_\_\_\_

$r$ : \_\_\_\_\_

9.  $p \vee r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

10.  $\sim p \vee q$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

11.  $\sim q \wedge r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

12.  $p \wedge \sim r$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

13.  $\sim p \vee \sim q$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

14.  $\sim r \wedge q$ : \_\_\_\_\_  
\_\_\_\_\_ Truth Value: \_\_\_\_\_

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<h1>TRUTH TABLES</h1>	<p><b>Truth tables are a convenient way of organizing truth values of statements.</b> Complete the following <u>negation</u>, <u>conjunction</u>, and <u>disjunction</u> truth tables:</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: center; border: 1px solid black; padding: 5px;"><b>Negation</b></td> <td style="text-align: center; border: 1px solid black; padding: 5px;"><b>Conjunction</b></td> <td style="text-align: center; border: 1px solid black; padding: 5px;"><b>Disjunction</b></td> </tr> <tr> <td style="border: 1px solid black; padding: 5px;"> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>\sim p</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table> </td> <td style="border: 1px solid black; padding: 5px;"> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>q</math></td><td style="border: 1px solid black; padding: 2px;"><math>p \wedge q</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table> </td> <td style="border: 1px solid black; padding: 5px;"> <table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>q</math></td><td style="border: 1px solid black; padding: 2px;"><math>p \vee q</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table> </td> </tr> </table> <p><b>Tips for Constructing Truth Tables:</b></p> <ul style="list-style-type: none"> <li>✓ Include columns for each statement involved. (<math>p, q, r</math>, etc.)</li> <li>✓ Include columns for any negations required. (<math>\sim p, \sim q, \sim r</math>, etc.).</li> <li>✓ Lastly, include columns for the compound statement(s).</li> </ul>	<b>Negation</b>	<b>Conjunction</b>	<b>Disjunction</b>	<table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>\sim p</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table>	$p$	$\sim p$	T		F		<table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>q</math></td><td style="border: 1px solid black; padding: 2px;"><math>p \wedge q</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table>	$p$	$q$	$p \wedge q$	T	T		T	F		F	T		F	F		<table style="width: 100%; border-collapse: collapse;"> <tr><td style="border: 1px solid black; padding: 2px;"><math>p</math></td><td style="border: 1px solid black; padding: 2px;"><math>q</math></td><td style="border: 1px solid black; padding: 2px;"><math>p \vee q</math></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">T</td><td style="border: 1px solid black; padding: 2px;"></td></tr> <tr><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;">F</td><td style="border: 1px solid black; padding: 2px;"></td></tr> </table>	$p$	$q$	$p \vee q$	T	T		T	F		F	T		F	F	
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<h1>EXAMPLES</h1>	<b>Construct truth tables for the following compound statements.</b>			
	<b>1</b> $p \vee \sim r$	<b>2</b> $\sim p \wedge q$		
	<b>3</b> $\sim q \vee r$	<b>4</b> $\sim p \wedge \sim r$		

5  $\sim p \vee \sim q$


6  $p \vee (q \wedge r)$


7  $\sim q \wedge (p \wedge r)$


8  $(\sim p \vee q) \wedge \sim r$
