

4-8**Study Guide and Intervention*****Least Common Multiple***

A **multiple** of a number is the product of that number and any whole number. The least nonzero multiple of two or more numbers is the **least common multiple (LCM)** of the numbers.

Example 1 Find the LCM of 15 and 20 by listing multiples.

List the multiples.

multiples of 15: 15, 30, 45, **60**, 75, 90, 105, **120**, ...

multiples of 20: 20, 40, **60**, 80, 100, **120**, 140, ...

Notice that 60, 120, ..., are common multiples. So, the LCM of 15 and 20 is 60.

Example 2 Find the LCM of 8 and 12 using prime factors.

Write the prime factorization.

$$8 = 2 \times 2 \times 2 = 2^3$$

$$12 = 2 \times 2 \times 3 = 2^2 \times 3$$

The prime factors of 8 and 12 are 2 and 3.
Multiply the greatest power of both 2 and 3.

The LCM of 8 and 12 is $2^3 \times 3$, or 24.

Exercises

Find the LCM of each set of numbers.

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|-----------------------|-----------------------|
| 1. 4, 6 12 | 2. 6, 9 18 |
| 3. 5, 9 45 | 4. 8, 10 40 |
| 5. 12, 15 60 | 6. 15, 21 105 |
| 7. 4, 15 60 | 8. 8, 20 40 |
| 9. 8, 16 16 | 10. 6, 14 42 |
| 11. 12, 20 60 | 12. 9, 12 36 |
| 13. 14, 21 42 | 14. 6, 15 30 |
| 15. 4, 6, 8 24 | 16. 3, 5, 6 30 |